CLASSICAL ELECTRODYNAMICS I

Homework Set 1 January 23, 2015

- 1. Consider a uniformly charged spherical shell of negligible thickness, radius R, and total charge Q.
 - (a) The charge density as a function of radial distance r can be written in various forms, e.g.: (i) $\rho(r) \propto \delta(r-R)$; (ii) $\rho(r) \propto \delta(r/R-1)$; (iii) $\rho(r) \propto \delta(r^2-R^2)$; (iv) $\rho(r) \propto \delta(r^2/R^2-1)$. Determine the correctly normalized proportionality constants in each case.
 - (b) Use your results from part (a) to determine a correctly normally expression for the charge density of a uniformly charged *ellipsoidal* shell of negligible thickness, with semimajor axes a, b, and c, and total charge Q.
- 2. Using one-dimensional Dirac delta functions and, where appropriate, the step function defined as

$$\Theta(x) \equiv \int_{-\infty}^{x} \delta(x) \ dx = \begin{cases} 0 & \text{if } x < 0 \\ 1 & \text{if } x > 0 \end{cases}$$

express the following charge distributions as three-dimensional charge densities $\rho(\mathbf{r})$:

- (a) In cylindrical coordinates, a charge λ per unit length uniformly distributed over a cylindrical surface of radius b;
- (b) In cylindrical coordinates, a charge Q spread uniformly over a flat circular disk of negligible thickness and radius R;
- (c) In spherical coordinates, a charge Q spread uniformly over a flat circular disk of negligible thickness and radius R.

Note that $d\Theta(x)/dx = \delta(x)$.